IRAM-30m HERA time/sensitivity estimator

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Abstract

This memo describes the equations used in the IRAM-30m HERA time/sensitivity estimator available on the IRAM-30m web page. A large part of the memo aims at describing the peculiarities of time/sensitivity estimation of the On-The-Fly observing mode with a multi-pixel like HERA. It explains how to generalize the equations of the single pixel case, so that the same code can be used in both cases (single and multi-pixel).

1 Summary of the formulas for a single pixel receiver

We summarize here the relations between the rms noise (σ) and the elapsed telescope time (t_{tel}) derived by Pety et al. (2009) in the case of a single-pixel heterodyne receiver. The results depends on a combination of

- The observation kind:

  Tracked observations where the telescope track the source, *i.e.* it always observes the same position in the source referential. The result is a single spectra.

  On-The-Fly observations where the telescope continuously slew through the source with time to map it. The result is a cube of spectra.

- and of the switching mode:

  Position switch where the off-measurement is done on a close-by sky position devoid of signal. Wobbler switching is a particular case.

  Frequency switch where the telescope always points towards the the source and the switching is done in the frequency (velocity) space. In this case,

The formulas are

- for tracked observations

$$\sigma_{\mathrm{psw}}^{\mathrm{track}} = \frac{2\,T_{\mathrm{sys}}}{\eta_{\mathrm{spec}}\sqrt{d\nu\,n_{\mathrm{pol}}\,\eta_{\mathrm{tel}}\,t_{\mathrm{tel}}}}, \quad \text{and} \quad \sigma_{\mathrm{fsw}}^{\mathrm{track}} = \frac{\sqrt{2}\,T_{\mathrm{sys}}}{\eta_{\mathrm{spec}}\sqrt{d\nu\,n_{\mathrm{pol}}\,\eta_{\mathrm{tel}}\,t_{\mathrm{tel}}}}. \tag{1}$$

- for OTF observations

$$\sigma_{\mathrm{psw}}^{\mathrm{otf}} = \frac{\left(\sqrt{n_{\mathrm{beam}}} + \sqrt{n_{\mathrm{submap}}}\right)\,T_{\mathrm{sys}}}{\eta_{\mathrm{spec}}\,\sqrt{d\nu\,n_{\mathrm{pol}}\,\eta_{\mathrm{tel}}\,t_{\mathrm{tel}}}}, \quad \text{and} \quad \sigma_{\mathrm{fsw}}^{\mathrm{otf}} = \frac{\sqrt{2\,n_{\mathrm{beam}}}\,T_{\mathrm{sys}}}{\eta_{\mathrm{spec}}\sqrt{d\nu\,n_{\mathrm{pol}}\,\eta_{\mathrm{tel}}\,t_{\mathrm{tel}}}}. \tag{2}$$

In these formulas

- η_{tel} is the efficiency of the telescope. It includes the time needed 1) to do calibrations (*e.g.* pointing, focus, temperature scale calibration), and 2) to slew the telescope between useful integrations, etc... Its value is decided by IRAM: It should *not* be changed by the PI.

- η_{spec} is the spectrometer efficiency.

- $d\nu$ is the frequency resolution.

- n_{pol} is the number of polarizations tuned at the same frequency (1 or 2).

- T_{sys} is the system temperature, which is a summary of the noise added by the system. It is usual to approximate it (in the $T_{\mathrm{a}}^{\star}$ scale) with

$$T_{\mathrm{sys}} = \frac{(1 + G_{\mathrm{im}}) \exp\{\tau_{\mathrm{s}}\,A\}}{F_{\mathrm{eff}}} \left[F_{\mathrm{eff}}\,T_{\mathrm{atm}}\,\left(1 - \exp\{-\tau_{\mathrm{s}}\,A\}\right) + (1 - F_{\mathrm{eff}})\,T_{\mathrm{cab}} + T_{\mathrm{rec}}\right], \qquad (3)$$

  where G_{im} is the receiver image gain, F_{eff} the telescope forward efficiency, $A = 1/\sin(\mathrm{elevation})$ the airmass, τ_{s} the atmospheric opacity in the signal band, T_{atm} the mean physical atmospheric temperature, T_{cab} the ambient temperature in the receiver cabine and T_{rec} the noise equivalent temperature of the receiver and the optics.

- n_{beam} is the number of independent measurement in the map observed in the OTF mode. It is given by

$$n_{\mathrm{beam}} = \frac{A_{\mathrm{map}}}{A_{\mathrm{beam}}} \quad \text{with} \quad A_{\mathrm{beam}} = \frac{\eta_{\mathrm{grid}}\,\pi\,\theta^2}{4\,\ln(2)}. \qquad (4)$$

  where A_{map} is the map area, A_{beam} is the area of the resolution element in the map, η_{grid} is the smoothing factor due to gridding and θ is the telescope full width at half maximum.

- n_{submap} the number of submaps needed to cover the whole map area, a submap being the area covered between two successive off measurements. n_{submap} is computed with

$$n_{\mathrm{submap}} = \frac{A_{\mathrm{map}}}{A_{\mathrm{submap}}} \quad \text{with} \quad A_{\mathrm{submap}} = \frac{\theta}{2.5}\,v_{\mathrm{linear}}\,t_{\mathrm{stable}} \qquad (5)$$

  where v_{linear} is the telescope scanning speed and t_{stable} is the typical timescale of stability of the observing system.

The demonstrations and additional subtleties for the OTF case are fully described in Pety et al. (2009).

2 Generalization to a multi-pixel receiver

2.1 Description of HERA, the IRAM-30m multi-pixels

HERA is a multi-pixel receiver working at 1 mm of wavelength. Each pixel is an heterodyne mixer using a SIS junction. There are nine pixels per polarization. The pixels of one polarization follow a 3×3 square pattern, the distance between two pixels being $\Delta = 24''$. Both polarizations are aligned. Hence, HERA has 18 pixels in total looking at 9 different sky position simultaneously. The polarizations of HERA can simultaneously be tuned at two different frequencies.

The number of used polarization, n_{pol} can thus be set to 1 or 2 and the number of pixels per polarization is $n_{\mathrm{pix}} = 9$.

2.2   An average pixel

The scatter of the mixer performances, which translate into a scatter of receiver temperatures, is the first thing to deal with. Instead of computing the sensitivity associated with each mixer, we introduce an average pixel, which will represent all the other ones. In Eqs. 1 and 2, the caracteristics of the mixers are hidden into the system temparature, T_{sys}. We will thus define an average system temperature, $\overline{T}_{\text{sys}}$, which will represent the receiver average pixel.

Among the different ways to define such an average system temperature, we priviledge the one which will give the right sensitivity in the case where the same point of the sky is seen by all the different pixels. This choice is made because 1) the same point of the sky is at least seen by two pixels (one per polarization) and 2) it is a good idea when mapping to try to cover the mapped area as many time as possible with sligthly different observing configuration of HERA (*e.g.* rotations by 90deg) to homogenize the noise distribution and to ensure that bad pixels see different part of the mapped area.

It is well-known that the optimal way to combine (*e.g.* to average or to grid) spectra is to weight them by $w = 1/\sigma^2$ before combination, where σ is their rms noise. In this case, it can be shown that the weight of the combination is the linear sum of the weights. From this, it is easy to define $\overline{T}_{\text{sys}}$ as

$$\frac{n_{\text{pol}}\, n_{\text{pix}}}{\overline{T}_{\text{sys}}^2} = \sum_{i=1,n_{\text{pol}},\, j=1,n_{\text{pix}}} \frac{1}{T_{\text{sys}_{ij}}^2}. \tag{6}$$

2.3   Impact on tracked observations

During tracked observations, each pixel of one polarization will look at a different position of the sky, but always the same position with time. We thus simply have to change T_{sys} by $\overline{T}_{\text{sys}}$ in Eqs. 1, *i.e.*

$$\sigma_{\text{psw}}^{\text{track}} = \frac{2\,\overline{T}_{\text{sys}}}{\eta_{\text{spec}}\sqrt{d\nu\, n_{\text{pol}}\, \eta_{\text{tel}}\, t_{\text{tel}}}}, \quad \text{and} \quad \sigma_{\text{fsw}}^{\text{track}} = \frac{\sqrt{2}\,\overline{T}_{\text{sys}}}{\eta_{\text{spec}}\sqrt{d\nu\, n_{\text{pol}}\, \eta_{\text{tel}}\, t_{\text{tel}}}}. \tag{7}$$

2.4   Imaging with HERA

HERA has a derotator, which ensures that the pixels do not rotate on the sky. The sky can thus be mapped by scanning along *e.g.* the right ascension or the declination axis in equatorial coordinates. We aim at obtaining a fully sampled map, implying a distance between the rows of $\Delta = \theta/2.5$, where θ is the beam full width at half maximum: At 1 mm, this corresponds typically to $4''$. However, the pixels are typically separated by $\Delta \simeq 2\theta$. We thus have to find the best scanning strategy which will fill the hole of the instantaneous footprint of the multi-pixel. To do this, we will use a property of the deroratator, *i.e.* it can be configured so that one of the main axes of the multi-pixel is rotated by an angle (α) from the scanning direction. Indeed, we can ask what is the value of α needed so that the distance between the rows of two adjacent pixels is exactly Δ. For a receiver of $\sqrt{n_{\text{pix}}} \times \sqrt{n_{\text{pix}}}$ pixels, we end up with $\sqrt{n_{\text{pix}}}$ groups of lines, the distance between two group of lines being noted δ'. A bit of geometry gives

$$\delta = \Delta \sin \alpha \quad \text{and} \quad \delta' = \Delta \cos \alpha. \tag{8}$$

If we now impose that

$$\delta' = n_{\text{subscan}} \sqrt{n_{\text{pix}}}\, \delta, \tag{9}$$

we obtain

$$\tan \alpha = \frac{1}{n_{\text{subscan}} \sqrt{n_{\text{pix}}}}. \tag{10}$$

We can fully sample without redundancy a given fraction of the sky in a single subscan ($n_{\text{subscan}} = 1$) or in two parallel subscans (zigzag, $n_{\text{subscan}} = 2$).

For HERA, $\sqrt{n_{\text{pix}}} = 3$ and the Δ value is fixed to $4''$ by the observing wavelenght ~ 1 mm. $n_{\text{subscan}} = 1$ gives $\alpha = 18.4°$, $\Delta \sim 12''$ and $n_{\text{subscan}} = 2$ gives $\alpha = 9.5°$, $\Delta \sim 24''$. Current optical design implies a minimum distance between the pixels which is only compatible with the $n_{\text{subscan}} = 2$ solution.

In summary, by setting an angle of $9.5°$ between one of the main axes of a 3×3 multi-pixels and the scanning direction, we can sweep in a fully sampled mode a given portion of the sky with two parallel scans separated by $3\delta = 12''$. The region of the sky fully sampled will then be rectangular: the length of the rectangular side perpendicular to the scanning direction is then $d_\perp = n_{\mathrm{subscan}} n_{\mathrm{pix}} \delta$, while the length of the rectangular size parallel to the scanning direction, $d_\parallel$, will depend on the observing strategy. However, there is an edge effect, due to the rotation of the array from the scanning direction. Indeed, the edges of the maps are not fully sampled: Thus must thus be considered as overheads. The area of the scanned sky must thus be larger than the targeted area, which must be fully sampled. Let's assume that the targeted area (A_{target}) is swept as a succession of $n_\perp$ rectangles of size $d_\perp \times d_\parallel$. We get

$$A_{\mathrm{target}} = n_\perp \, d_\perp \, d_\parallel. \tag{11}$$

The area swept in the under-sampled edges (A_{edge}) is just the area of the rectangle whose side sizes are $n_\perp \, d_\perp$ and the scanning size of multi-pixel rotated by α, *i.e.*

$$d_{\mathrm{edge}} = (\sqrt{n_{\mathrm{pix}}} - 1) \, \Delta \, (\cos\alpha + \sin\alpha) \tag{12}$$

Indeed, the geometry of the edges show that half this area is covered on each size of the targeted area. Using Eqs. 8 and 9, we obtain

$$d_{\mathrm{edge}} = (\sqrt{n_{\mathrm{pix}}} - 1) \, (1 + n_{\mathrm{subscan}} \sqrt{n_{\mathrm{pix}}}) \delta \tag{13}$$

We now define the mapping efficiency η_{edge} as

$$\eta_{\mathrm{edge}} = \frac{A_{\mathrm{target}}}{A_{\mathrm{target}} + A_{\mathrm{edge}}}, \quad \text{with} \quad A_{\mathrm{edge}} = n_\perp \, d_\perp \, d_{\mathrm{edge}}. \tag{14}$$

Replacing A_{target} and A_{edge} by their expressions 11 and 14, we derive

$$\eta_{\mathrm{edge}} = \frac{1}{1 + \frac{d_{\mathrm{edge}}}{d_\parallel}} = \frac{1}{1 + \frac{d_{\mathrm{edge}}}{a \, n_\perp \, d_\perp}}. \tag{15}$$

This expression indicates that the most efficient mapping strategy is to observe very wide scans. However, avoiding the edge overheads is only one aspect of wide-field mapping with a multi-pixels. In particular, we aim at having the most homogeneous map as possible. To achieve this, we need to scan as fast as possible so that the observing conditions are as comparable as possible on the whole map. We can then repeat the map as many time as possible so that the data affected by technical problems or bad weather happening during one coverage can just be discarded. In any case, at least two coverages obtained in perpendicular scanning direction is always advise to be able to use destriping algorithms (*e.g.* plait algorithms). Stripes happen because the system stability (weather, telescope, receiver and backend) evolves from one row to the other. Getting stripes is all the more probable than the time to scan a row is long. So this argues against making very wide scans, which are at the same time required to decrease the relative time spent in the edge overheads. A compromise is thus to map area chunks which are as close as possible to squares. A way to parametrize this is to introduce the map aspect ratio, defined as

$$a = \frac{d_\parallel}{n_\perp \, d_\perp} \quad \text{with} \quad a > 1 \quad \text{and} \quad n_\perp \text{ integer.} \tag{16}$$

A given area A_{map} will be mapped in chunks whose area (A_{chunk}) is defined by the linear scanning speed and the time of stability of the system (t_{chunk}). This gives

$$n_\perp \, d_\perp \, (d_\parallel + d_{\mathrm{edge}}) = A_{\mathrm{chunk}} \quad \text{with} \quad A_{\mathrm{chunk}} = v_{\mathrm{linear}} \, d_\perp \, t_{\mathrm{chunk}}. \tag{17}$$

Using 16 to replace $d_\parallel$ by $a \, n_\perp \, d_\perp$, we yield

$$n_\perp^2 + n_\perp \, \frac{d_{\mathrm{edge}}}{a \, d_\perp} - \frac{A_{\mathrm{chunk}}}{a \, d_\perp^2} = 0. \tag{18}$$

Table 1: Mapping strategy to minimize edge effects.

t_{chunk} min.	$n_\perp$	a	η_{edge}
1	1	3.7	0.83
2	2	1.9	0.83
5	4	1.2	0.86
10	6	1.1	0.90

This equation of the 2nd order has only one physical solution

$$n_\perp = \frac{1}{2} \frac{d_{\text{edge}}}{a\, d_\perp} \left[\sqrt{1 + \frac{4a\, A_{\text{chunk}}}{d_{\text{edge}}^2}} - 1 \right]. \tag{19}$$

We note that this yields

$$\eta_{\text{edge}} = \frac{1}{1 + \frac{2}{\sqrt{1 + \frac{4a\, A_{\text{chunk}}}{d_{\text{edge}}^2}} - 1}} \tag{20}$$

$$\text{with} \quad \frac{a\, A_{\text{chunk}}}{d_{\text{edge}}^2} = \frac{\theta}{4\delta} \frac{a\, f_{\text{dump}} t_{\text{chunk}}}{\left[\left(\sqrt{n_{\text{subscan}}\, n_{\text{pix}}} - \frac{1}{\sqrt{n_{\text{subscan}}\, n_{\text{pix}}}} \right) - \left(\sqrt{n_{\text{subscan}}} - \frac{1}{\sqrt{n_{\text{subscan}}}} \right) \right]^2}. \tag{21}$$

This expression can be used to understand how to get the highest mapping effiency (η_{edge}). This implies to get the largest value of the $(a\, A_{\text{chunk}})/d_{\text{edge}}^2$ ratio. We see that the larger the multi-pixel array, the smaller this ratio. Increasing the chunk area, either by increasing the linear velocity (*i.e.* increasing the dump rate, f_{dump}) or by increasing the stability time (t_{chunk}) will increase the efficiency. The dump rate is fixed by the peak data rate, which gives typically $f_{\text{dump}} = 2$ Hz. The stability time depends on the switching mode: It is the time between two off measurements in position switch (typically 1 or 2 minutes) and the time between two calibrations in frequency switch (typically 10 to 15 minutes).

Previous equations give the impression that the aspect ratio is a free parameter. This is not fully true because, $n_\perp$ must be an integer. The following algorithm ensures that we get an integer value for $n_\perp$ with the value of $a > 1$ and closest to 1. Starting with $a = 1$, Eq. 18 gives a value of $n_\perp$. We enforce the integer nature of $n_\perp$ with

$$n_\perp = \text{floor}(n_\perp), \tag{22}$$

and we recompute the associated aspect ratio with

$$a = \frac{A_{\text{chunk}}}{(n_\perp\, d_\perp)^2} - \frac{d_{\text{edge}}}{n_\perp\, d_\perp}. \tag{23}$$

Table 1 gives the resulting values of $n_\perp$, a and η_{edge} as a function of the stability time (t_{chunk}). We see that edge efficiencies are quite high. However, it is easier to have square chunks when the stability time is larger.

In summary, the time spent in edges is counted as overheads. It translates into a multiplicative efficiency (η_{edge}) because we enforce a mapping pattern through rectangular chunks. Although it is not intuitive (edge sizes are in general unrelated to area), this is not a big assumption because the use of a square multi-pixel anyway enforces mapping in rectangular chunks. We now summarize the algorithm to compute η_{edge}:

Step #1: Computation of input quantities

$$d_\perp = n_{\text{subscan}}\, n_{\text{pix}}\, \delta, \tag{24}$$

$$d_{\text{edge}} = (\sqrt{n_{\text{pix}}} - 1)(1 + n_{\text{subscan}}\sqrt{n_{\text{pix}}})\delta, \tag{25}$$

$$t_{\text{chunk}}^{\text{psw}} = 2 \text{ minutes} \quad \text{and} \quad t_{\text{chunk}}^{\text{fsw}} = 10 \text{ minutes}. \tag{26}$$

$$A_{\text{chunk}} = \frac{\theta}{4} f_{\text{dump}} \frac{d_\perp}{n_{\text{subscan}}} t_{\text{chunk}}. \tag{27}$$

Step #2: Computation of $n_\perp$ and a

Case $A_{\text{target}} < \eta_{\text{edge}}^{\text{min}} A_{\text{chunk}}$ with $\eta_{\text{edge}}^{\text{min}} = 0.8$

1. $$n_\perp = \text{floor}\left[\frac{\sqrt{A_{\text{target}}}}{d_\perp}\right], \tag{28}$$

2. if $n_\perp = 0$, then send an error message: "Area too small, use raster mapping.", (29)

3. $$a = \frac{A_{\text{target}}}{(n_\perp d_\perp)^2}. \tag{30}$$

Case $A_{\text{target}} \geq \eta_{\text{edge}}^{\text{min}} A_{\text{chunk}}$

1. $$n_\perp = \text{floor}\left\{\frac{1}{2}\frac{d_{\text{edge}}}{d_\perp}\left[\sqrt{1 + \frac{4A_{\text{chunk}}}{d_{\text{edge}}^2}} - 1\right]\right\}, \tag{31}$$

2. if $n_\perp = 0$, then send an error message: "Area too small, use raster mapping.", (32)

3. $$a = \frac{A_{\text{chunk}}}{(n_\perp d_\perp)^2} - \frac{d_{\text{edge}}}{n_\perp d_\perp}. \tag{33}$$

Step #3: Computation of η_{edge}

$$\eta_{\text{edge}} = \frac{1}{1 + \frac{d_{\text{edge}}}{a\,n_\perp d_\perp}}. \tag{34}$$

Step #4: Recomputation of A_{chunk} and t_{chunk} when $A_{\text{target}} < \eta_{\text{edge}}^{\text{min}} A_{\text{chunk}}$

1. $$A_{\text{chunk}}^{\text{new}} = \frac{A_{\text{target}}}{\eta_{\text{edge}}}, \tag{35}$$

2. $$t_{\text{chunk}}^{\text{new}} = t_{\text{chunk}} \frac{A_{\text{chunk}}^{\text{new}}}{A_{\text{chunk}}}, \tag{36}$$

3. $$A_{\text{chunk}} = A_{\text{chunk}}^{\text{new}} \quad \text{and} \quad t_{\text{chunk}} = t_{\text{chunk}}^{\text{new}}. \tag{37}$$

If $t_{\text{chunk}} < 1$ minute, the targeted area is too small and the PI should use raster mapping instead of OTF mapping.

2.5 Impact on OTF observations

For OTF observations, there are several effects to take into account.

1. We will use the average system temperature to take into account the different mixer performances.

2. Edges result in inhomogeneous noise, which depends on the exact observing setup. We here try to estimate a single noise value for the whole map. The area swept in edges are thus considered as overheads. If the total targeted area is A_{map}, the receiver will then have to map $A_{\text{map}} + A_{\text{edge}}$. As discussed above, we can write the previous sum as a product of the targeted area times an efficiency factor, *i.e.*

$$\eta_{\text{edge}}(A_{\text{map}} + A_{\text{edge}}) = A_{\text{map}}. \tag{38}$$

We thus have to remplace A_{map} by $A_{\mathrm{map}}/\eta_{\mathrm{edge}}$ in Eqs 4 and 5 to compute n_{beam} and n_{submap}. Now, if edge area is considered overheads when estimating the sensitivity, the spectra acquired in the edges will nevertheless be used to form the final image. We must thus ensure that enough time is observed on the off position when estimating the sensitivity in the position switch mode. This comes naturally if we consider the edge area as part of the submap between two off positions. This implies that the change on the total mapped area, expressed above, is the only one needed in the equations to take the edges into account.

3. A multi-pixel can cover n_{pix} times as fast the same area of the sky with the same sensitivity as a single-pixel of similar $\overline{T}_{\mathrm{sys}}$. Another way to look at this, is to assume that each identical (average) pixel will cover an independent part of the sky during a given observing time (*i.e.* $\eta_{\mathrm{tel}}\, t_{\mathrm{tel}}$). This implies that the area seen by each pixel will be

$$A_{\mathrm{map}}^{\mathrm{pix}} = \frac{A_{\mathrm{map}}/\eta_{\mathrm{edge}}}{n_{\mathrm{pix}}}. \tag{39}$$

This finally gives

$$\sigma_{\mathrm{psw}}^{\mathrm{otf}} = \frac{\left(\sqrt{n_{\mathrm{beam}}^{\mathrm{pix}}} + \sqrt{n_{\mathrm{submap}}^{\mathrm{pix}}}\right)\overline{T}_{\mathrm{sys}}}{\eta_{\mathrm{spec}}\,\sqrt{d\nu\, n_{\mathrm{pol}}\,\eta_{\mathrm{tel}}\, t_{\mathrm{tel}}}}, \quad \text{and} \quad \sigma_{\mathrm{fsw}}^{\mathrm{otf}} = \frac{\sqrt{2\, n_{\mathrm{beam}}^{\mathrm{pix}}}\,\overline{T}_{\mathrm{sys}}}{\eta_{\mathrm{spec}}\,\sqrt{d\nu\, n_{\mathrm{pol}}\,\eta_{\mathrm{tel}}\, t_{\mathrm{tel}}}}, \tag{40}$$

where $n_{\mathrm{beam}}^{\mathrm{pix}}$ and $n_{\mathrm{submap}}^{\mathrm{pix}}$ are computed with

$$n_{\mathrm{beam}}^{\mathrm{pix}} = \frac{A_{\mathrm{map}}}{\eta_{\mathrm{edge}}\, n_{\mathrm{pix}}\, A_{\mathrm{beam}}} \quad \text{and} \quad n_{\mathrm{submap}}^{\mathrm{pix}} = \frac{A_{\mathrm{map}}}{\eta_{\mathrm{edge}}\, n_{\mathrm{pix}}\, A_{\mathrm{submap}}^{\mathrm{pix}}} \tag{41}$$

$$\text{with} \quad A_{\mathrm{submap}}^{\mathrm{pix}} = v_{\mathrm{area}}^{\mathrm{pix}}\, t_{\mathrm{stable}} \quad \text{and} \quad v_{\mathrm{area}}^{\mathrm{pix}} = \delta\, v_{\mathrm{linear}}. \tag{42}$$

The times spent on and off and in the edges per pixel are then

$$t_{\mathrm{onoff}}^{\mathrm{pix}} = \eta_{\mathrm{edge}}\, \eta_{\mathrm{tel}}\, t_{\mathrm{tel}} \quad \text{and} \quad t_{\mathrm{edge}}^{\mathrm{pix}} = (1 - \eta_{\mathrm{edge}})\, \eta_{\mathrm{tel}}\, t_{\mathrm{tel}}. \tag{43}$$

The algorithm to derive the time/sensitivity estimation in the case of OTF can thus be applied with the following modifications in the input parameters : t_{onoff}, v_{area}, n_{submap}, n_{beam} must be replaced by $t_{\mathrm{onoff}}^{\mathrm{pix}}$, $v_{\mathrm{area}}^{\mathrm{pix}}$, $n_{\mathrm{submap}}^{\mathrm{pix}}$, $n_{\mathrm{beam}}^{\mathrm{pix}}$.

References

Pety, J., Bardeau, S. and Reynier, E., 2009, IRAM-30m EMIR time/sensitivity estimator, IRAM Memo 2009-1